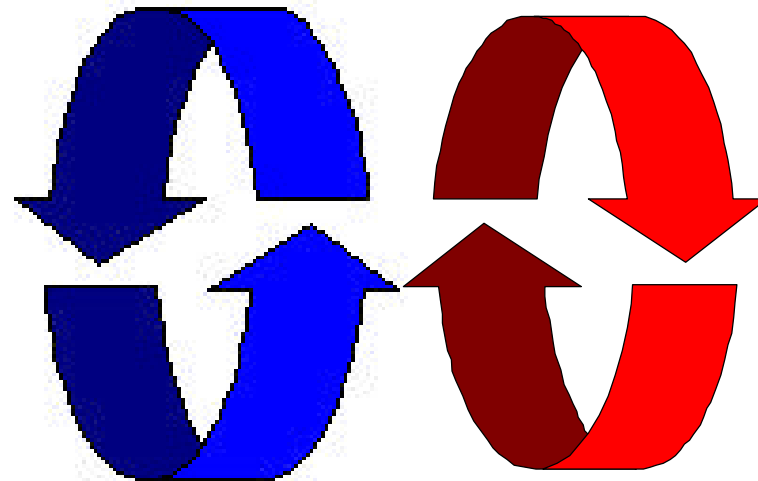


# Concurrent Execution



## Concurrent execution

---

**Concepts:** processes - concurrent execution  
and interleaving.  
process interaction.

**Models:** **parallel composition** of asynchronous processes  
- interleaving  
**interaction** - shared actions  
process labeling, and action relabeling and hiding  
**structure diagrams**

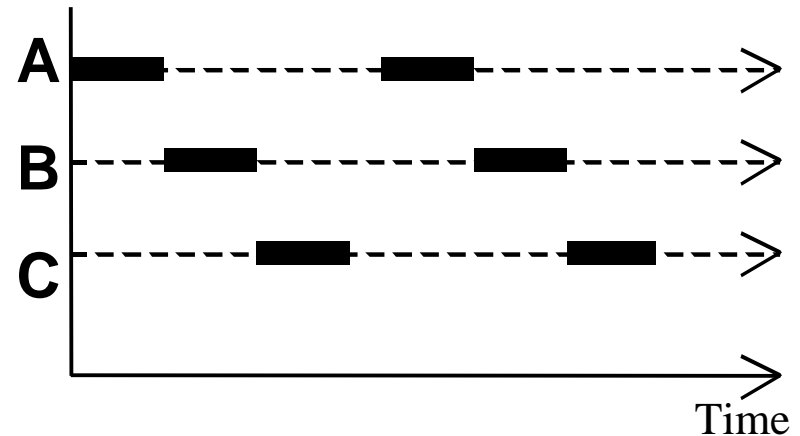
**Practice:** Multithreaded Java programs

# Definitions

---

## ◆ **Concurrency**

- *Logically* simultaneous processing. Does not imply multiple processing elements (PEs). Requires interleaved execution on a single PE.



## ◆ **Parallelism**

- *Physically* simultaneous processing. Involves multiple PEs and/or independent device operations.

Both concurrency and parallelism require controlled access to shared resources . We use the terms parallel and concurrent interchangeably and generally do not distinguish between real and pseudo-concurrent execution.

## 3.1 Modeling Concurrency

---

- ◆ How should we model process execution speed?
  - arbitrary speed  
(we abstract away time)
- ◆ How do we model concurrency?
  - arbitrary relative order of actions from different processes  
(**interleaving** but preservation of each process order )
- ◆ What is the result?
  - provides a general model independent of scheduling  
(**asynchronous** model of execution)

## parallel composition - action interleaving

---

If  $P$  and  $Q$  are processes then  $(P||Q)$  represents the concurrent execution of  $P$  and  $Q$ . The operator  $||$  is the parallel composition operator.

```
ITCH = (scratch->STOP).
```

```
CONVERSE = (think->talk->STOP).
```

```
||CONVERSE_ITCH = (ITCH || CONVERSE).
```

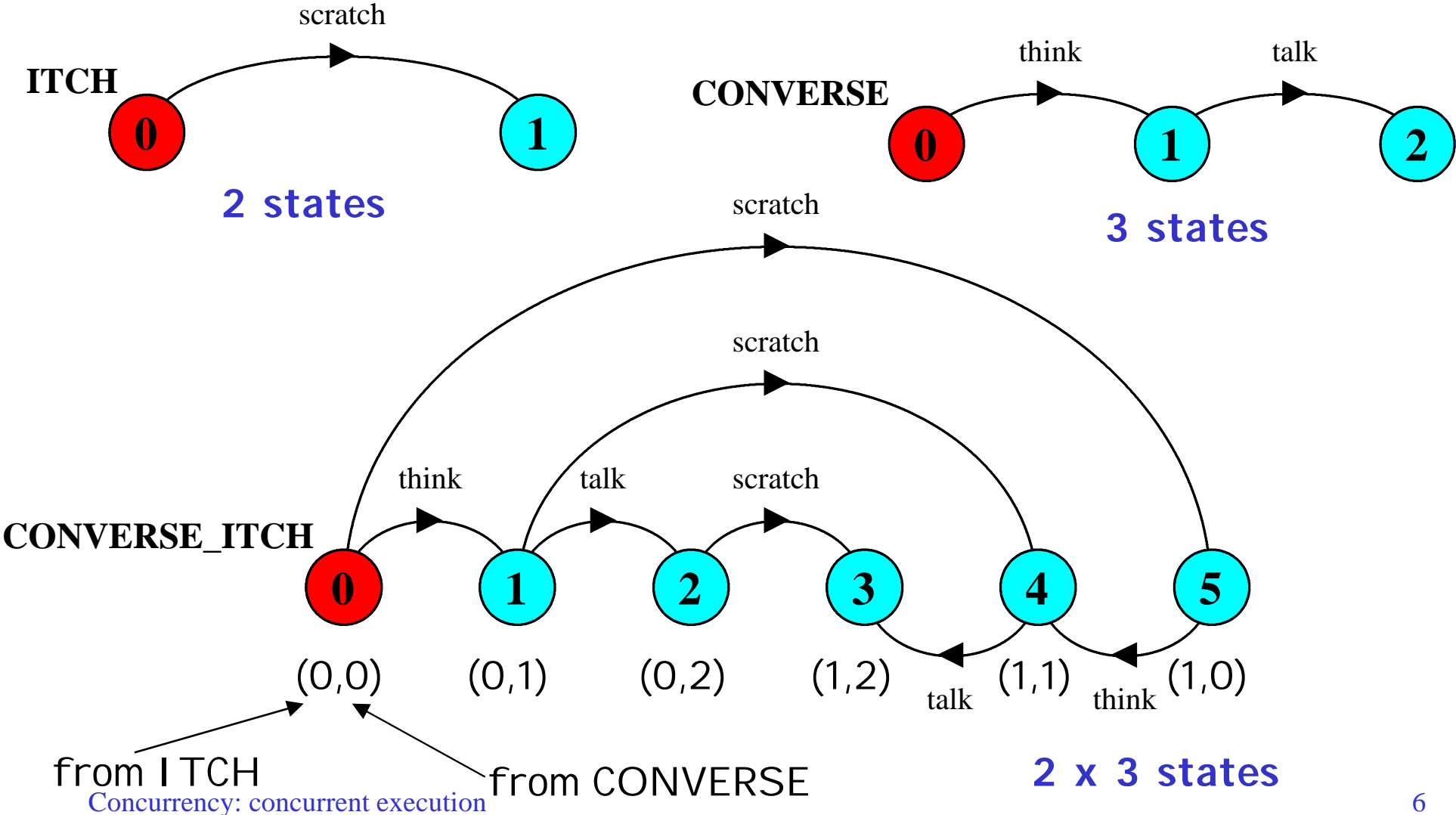
```
think talk scratch
```

```
think scratch talk
```

```
scratch think talk
```

Possible traces as  
a result of action  
interleaving.

# parallel composition - action interleaving



## parallel composition - algebraic laws

---

**Commutative:**  $(P \parallel Q) = (Q \parallel P)$

**Associative:**  $(P \parallel (Q \parallel R)) = ((P \parallel Q) \parallel R)$   
 $= (P \parallel Q \parallel R).$

Clock radio example:

**CLOCK = (tick->CLOCK).**

**RADIO = (on->off->RADIO).**

**$\parallel$ CLOCK\_RADIO = (CLOCK  $\parallel$  RADIO).**

***LTS? Traces? Number of states?***

## modeling interaction - shared actions

If processes in a composition have actions in common, these actions are said to be *shared*. Shared actions are the way that process interaction is modeled. While unshared actions may be arbitrarily interleaved, a shared action must be executed at the same time by all processes that participate in the shared action.

```
MAKER = (make->ready->MAKER) .
```

```
USER  = (ready->use->USER) .
```

```
||MAKER_USER = (MAKER || USER) .
```

**MAKER**

synchronizes  
with **USER**  
when **ready**.

*LTS? Traces? Number of states?*



## modeling interaction - handshake

A handshake is an action acknowledged by another:

```
MAKERv2 = (make->ready->used->MAKERv2) .
```

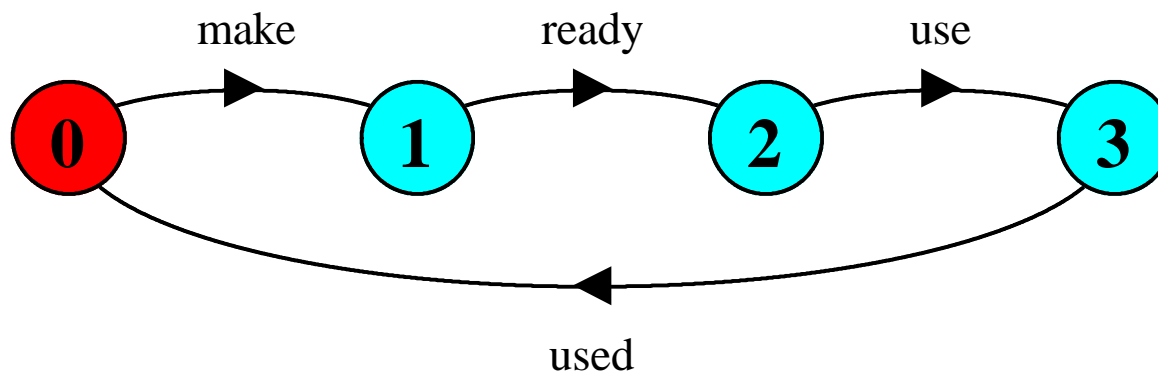
```
USERv2 = (ready->use->used->USERv2) .
```

```
||MAKER_USERv2 = (MAKERv2 || USERv2) .
```

3 states

3 states

3 x 3  
states?



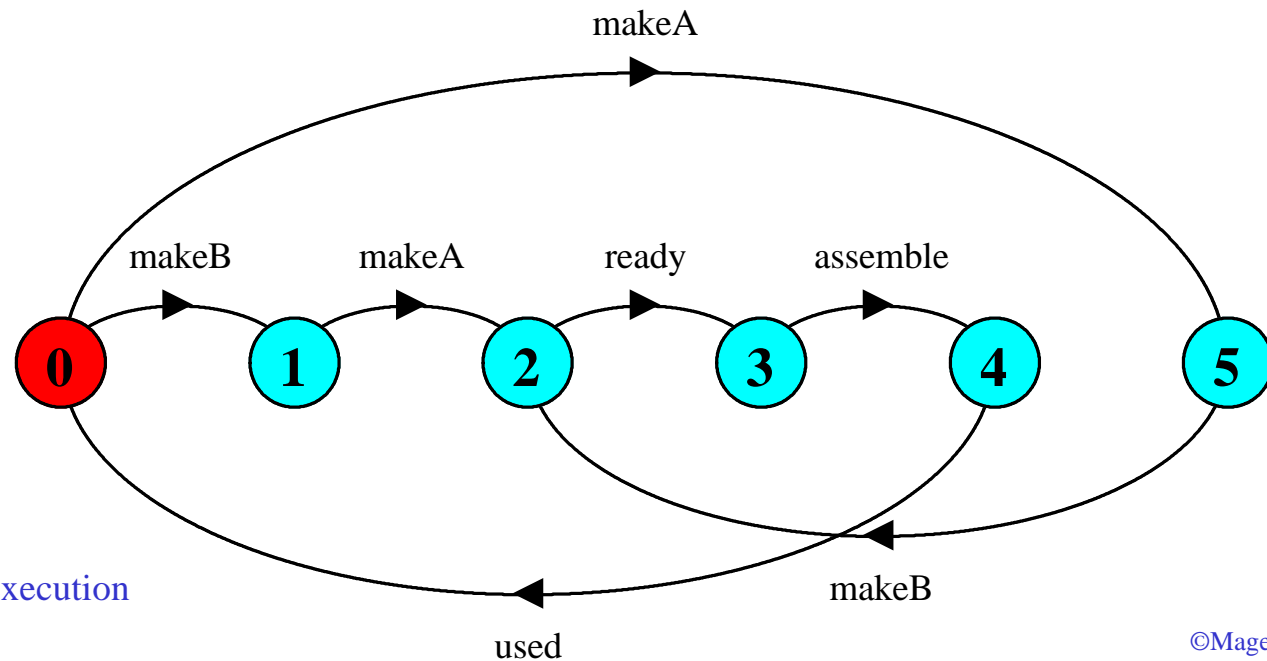
4 states

Interaction  
constrains  
the overall  
behaviour.

# modeling interaction - multiple processes

Multi-party synchronization:

```
MAKE_A    = (makeA->ready->used->MAKE_A) .  
MAKE_B    = (makeB->ready->used->MAKE_B) .  
ASSEMBLE  = (ready->assemble->used->ASSEMBLE) .  
||FACTORY = (MAKE_A || MAKE_B || ASSEMBLE) .
```



Concurrency: concurrent execution

## composite processes

---

A composite process is a parallel composition of primitive processes. These composite processes can be used in the definition of further compositions.

$$|| \text{MAKERS} = (\text{MAKE\_A} || \text{MAKE\_B}).$$
$$|| \text{FACTORY} = (\text{MAKERS} || \text{ASSEMBLE}).$$

Substituting the definition for **MAKERS** in **FACTORY** and applying the **commutative** and **associative** laws for parallel composition results in the original definition for **FACTORY** in terms of primitive processes.

$$|| \text{FACTORY} = (\text{MAKE\_A} || \text{MAKE\_B} || \text{ASSEMBLE}).$$

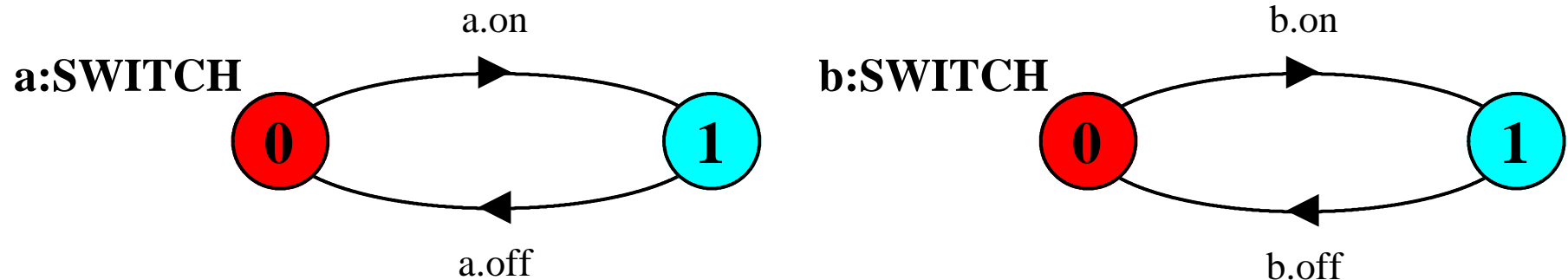
## process labeling

a:P prefixes each action label in the alphabet of P with a.

Two **instances** of a switch process:

**SWITCH** = (on->off->SWITCH).

|| **TWO\_SWITCH** = (a:SWITCH || b:SWITCH).



An array of **instances** of the switch process:

|| **SWITCHES(N=3)** = (forall[i:1..N] s[i]:SWITCH).

|| **SWITCHES(N=3)** = (s[i:1..N]:SWITCH).

## process labeling by a set of prefix labels

---

$\{a_1, \dots, a_x\}::P$  replaces every action label  $n$  in the alphabet of  $P$  with the labels  $a_1.n, \dots, a_x.n$ . Further, every transition  $(n \rightarrow X)$  in the definition of  $P$  is replaced with the transitions  $(\{a_1.n, \dots, a_x.n\} \rightarrow X)$ .

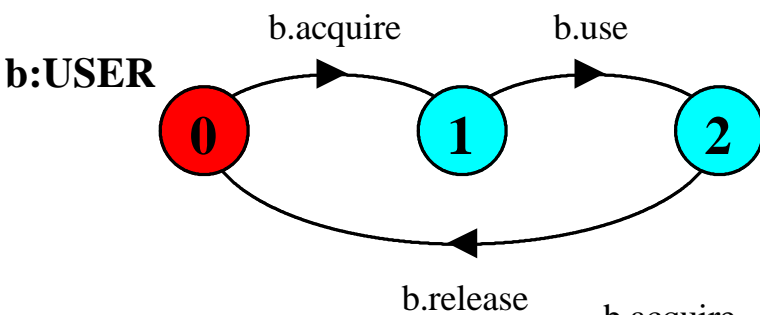
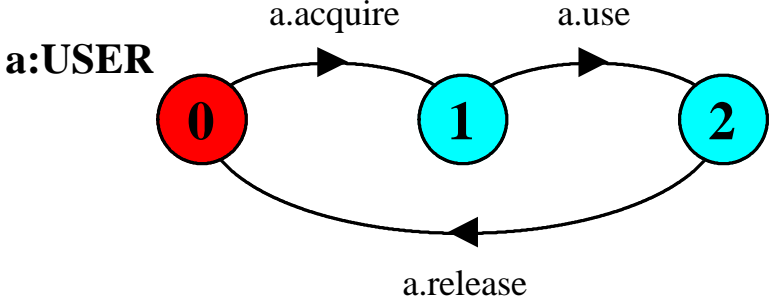
Process prefixing is useful for modeling **shared** resources:

**RESOURCE** = (**acquire**  $\rightarrow$  **release**  $\rightarrow$  **RESOURCE**) .

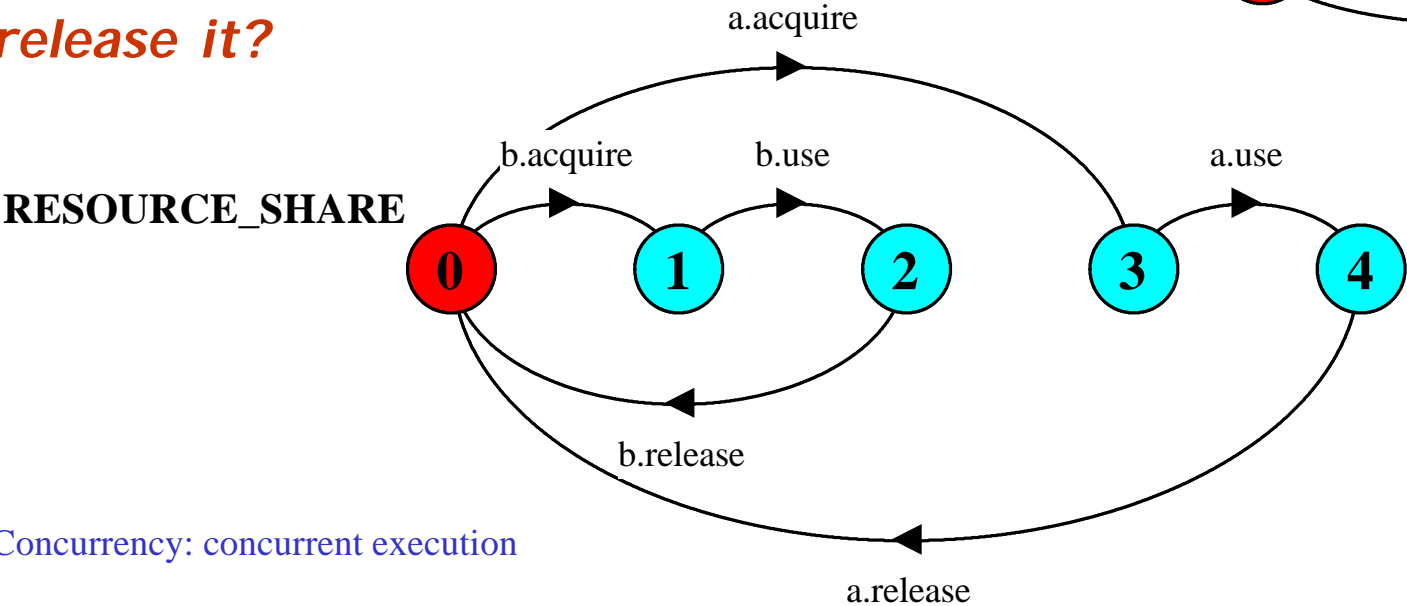
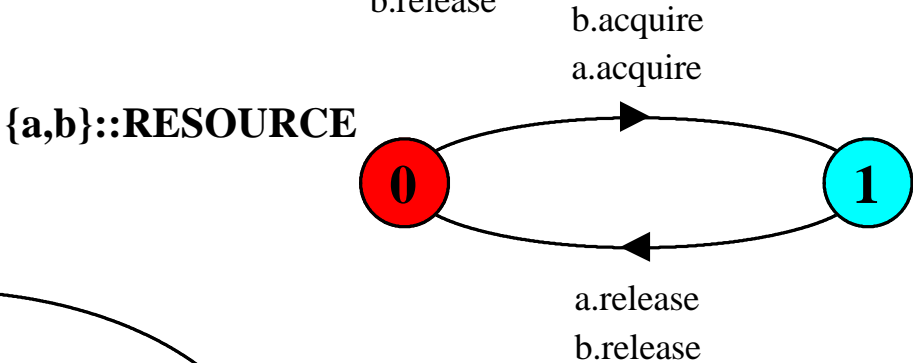
**USER** = (**acquire**  $\rightarrow$  **use**  $\rightarrow$  **release**  $\rightarrow$  **USER**) .

**RESOURCE\_SHARE** = (**a**:**USER** || **b**:**USER**  
|| **{a, b}**:**RESOURCE**) .

# process prefix labels for shared resources



*How does the model ensure that the user that acquires the resource is the one to release it?*



## action relabeling

---

Relabeling functions are applied to processes to change the names of action labels. The general form of the relabeling function is:

*/{newlabel\_1/oldlabel\_1,... newlabel\_n/oldlabel\_n}.*

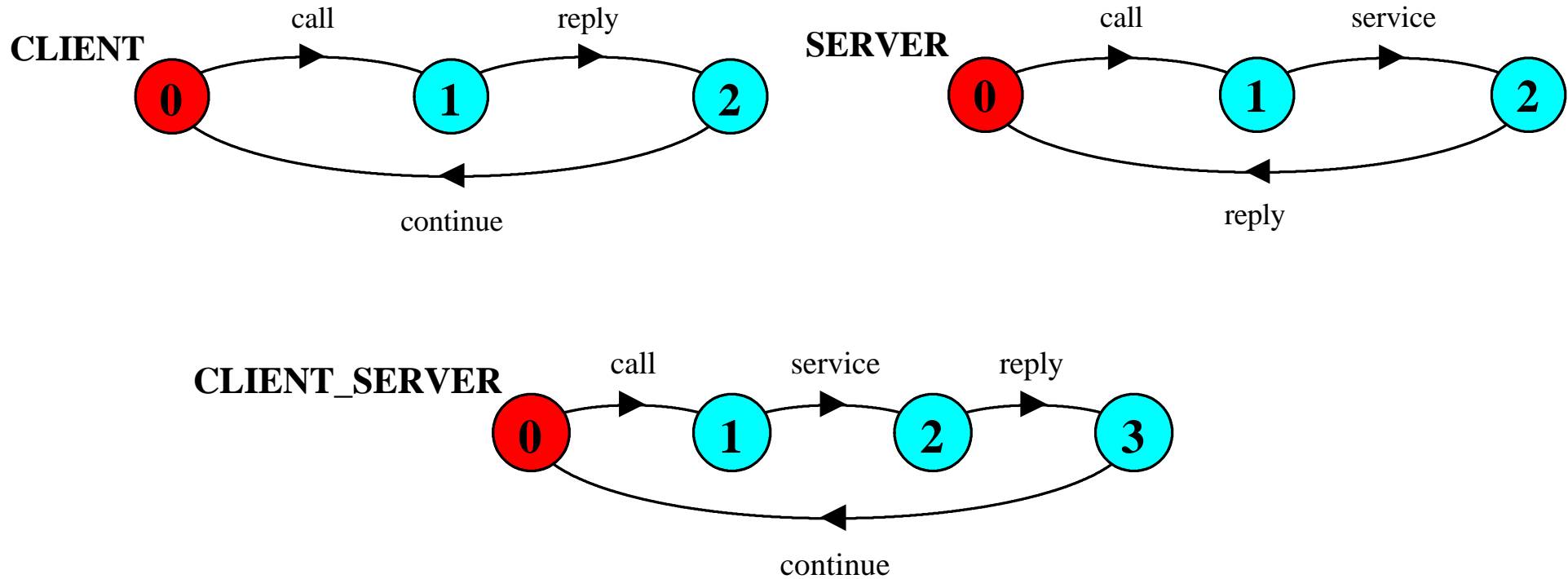
Relabeling to ensure that composed processes synchronize on particular actions.

**CLIENT** = (**call**->**wait**->**continue**->**CLIENT**).

**SERVER** = (**request**->**service**->**reply**->**SERVER**).

# action relabeling

$|| \text{CLIENT\_SERVER} = (\text{CLIENT} || \text{SERVER})$   
 $/ \{ \text{call/request}, \text{reply/wait} \}.$





## action relabeling - prefix labels

---

An alternative formulation of the client server system is described below using qualified or prefixed labels:

```
SERVERv2 = (accept.request
            ->service->accept.reply->SERVERv2).
CLIENTv2 = (call.request
            ->call.reply->continue->CLIENTv2).

|| CLIENT_SERVERv2 = (CLIENTv2 || SERVERv2)
                    / {call/accept}.
```

## action hiding - abstraction to reduce complexity

---

When applied to a process  $P$ , the hiding operator  $\backslash\{a1..ax\}$  removes the action names  $a1..ax$  from the alphabet of  $P$  and makes these concealed actions "silent". These silent actions are labeled **tau**. Silent actions in different processes are not shared.

Sometimes it is more convenient to specify the set of labels to be **exposed**....

When applied to a process  $P$ , the interface operator  $@\{a1..ax\}$  hides all actions in the alphabet of  $P$  not labeled in the set  $a1..ax$ .

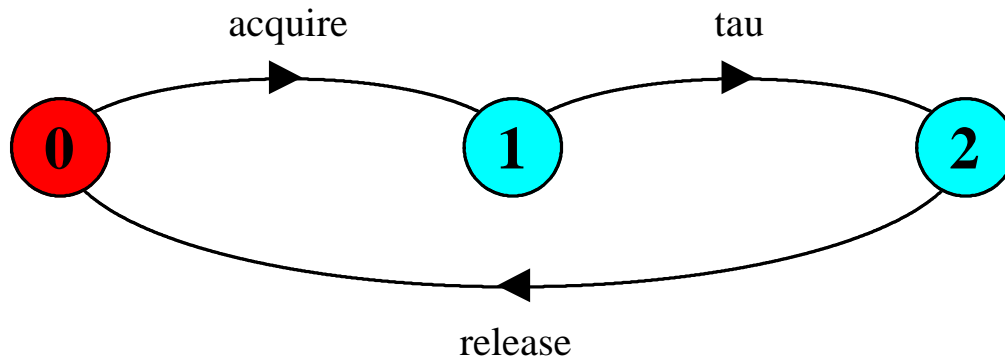
## action hiding

---

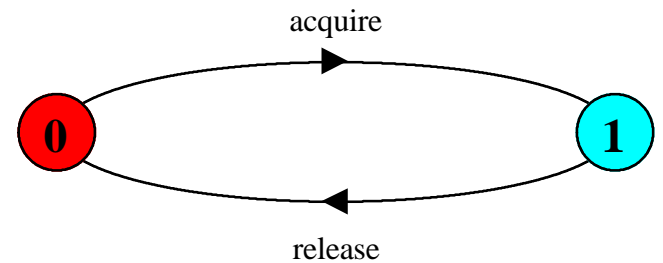
The following definitions are equivalent:

$$\text{USER} = (\text{acquire} \rightarrow \text{use} \rightarrow \text{release} \rightarrow \text{USER}) \setminus \{\text{use}\}.$$

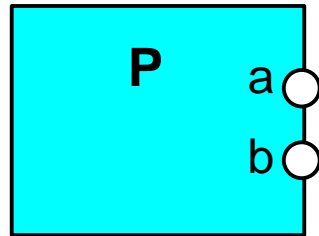
$$\text{USER} = (\text{acquire} \rightarrow \text{use} \rightarrow \text{release} \rightarrow \text{USER}) @ \{\text{acquire}, \text{release}\}.$$



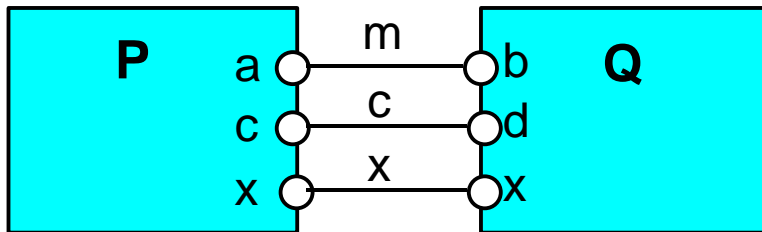
Minimization removes hidden **tau** actions to produce an LTS with equivalent observable behavior.



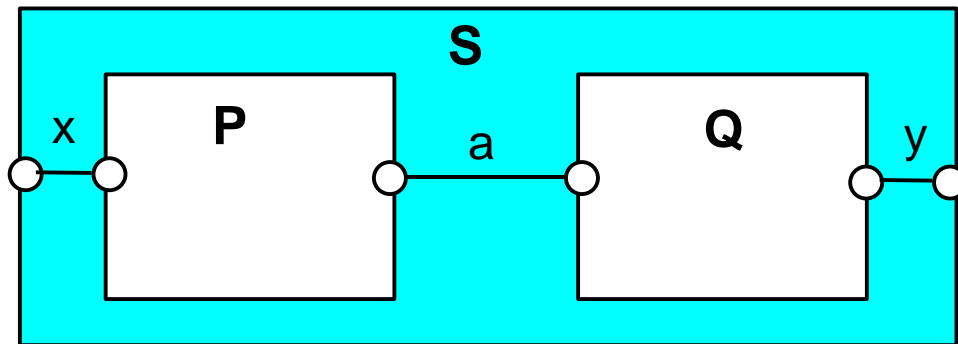
# structure diagrams



Process P with alphabet {a,b}.



Parallel Composition  $(P || Q) / \{m/a, m/b, c/d\}$



Composite process  $||S = (P || Q) @ \{x,y\}$

Concurrency: concurrent execution

## structure diagrams

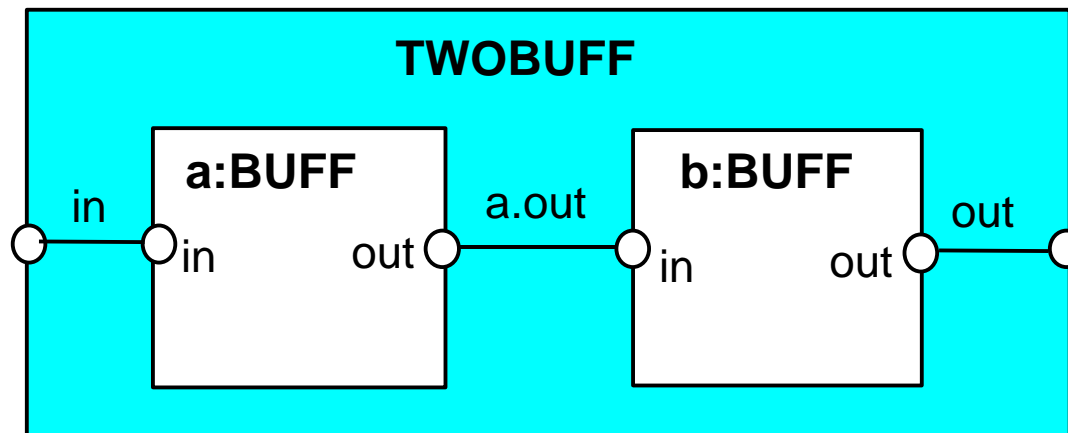
---

We use structure diagrams to capture the structure of a model expressed by the static combinators: *parallel composition*, *relabeling* and *hiding*.

**range T = 0..3**

**BUFF = (in[i:T]->out[i]->BUFF) .**

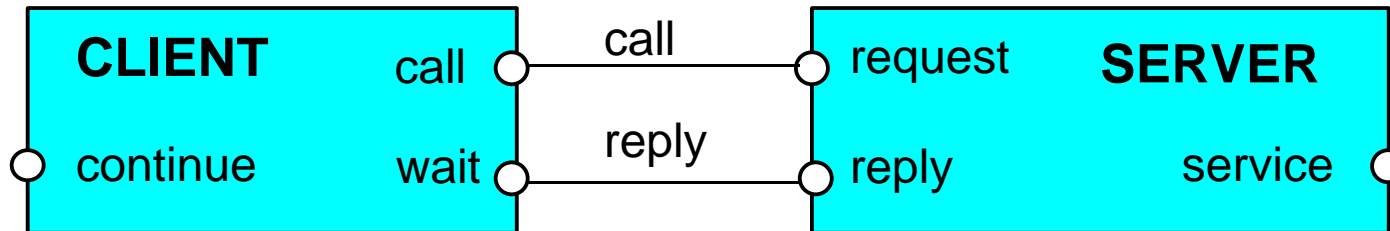
**| | TWOBUFF = ?**



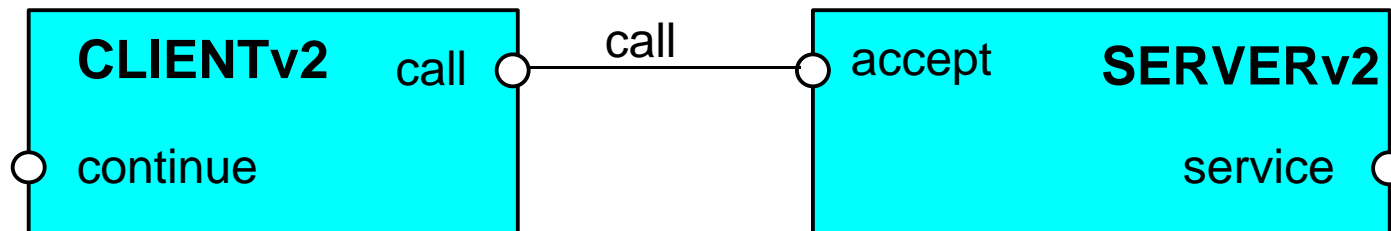
## structure diagrams

---

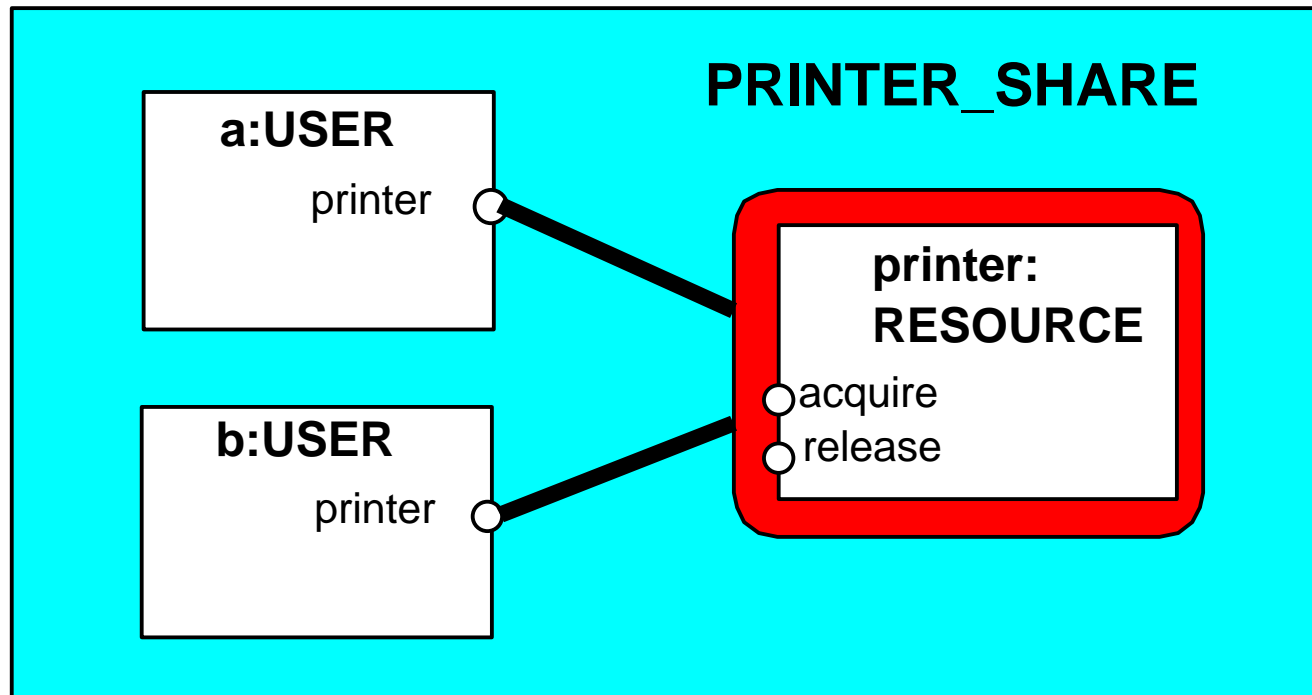
Structure diagram for **CLIENT\_SERVER** ?



Structure diagram for **CLIENT\_SERVERv2** ?



## structure diagrams - resource sharing



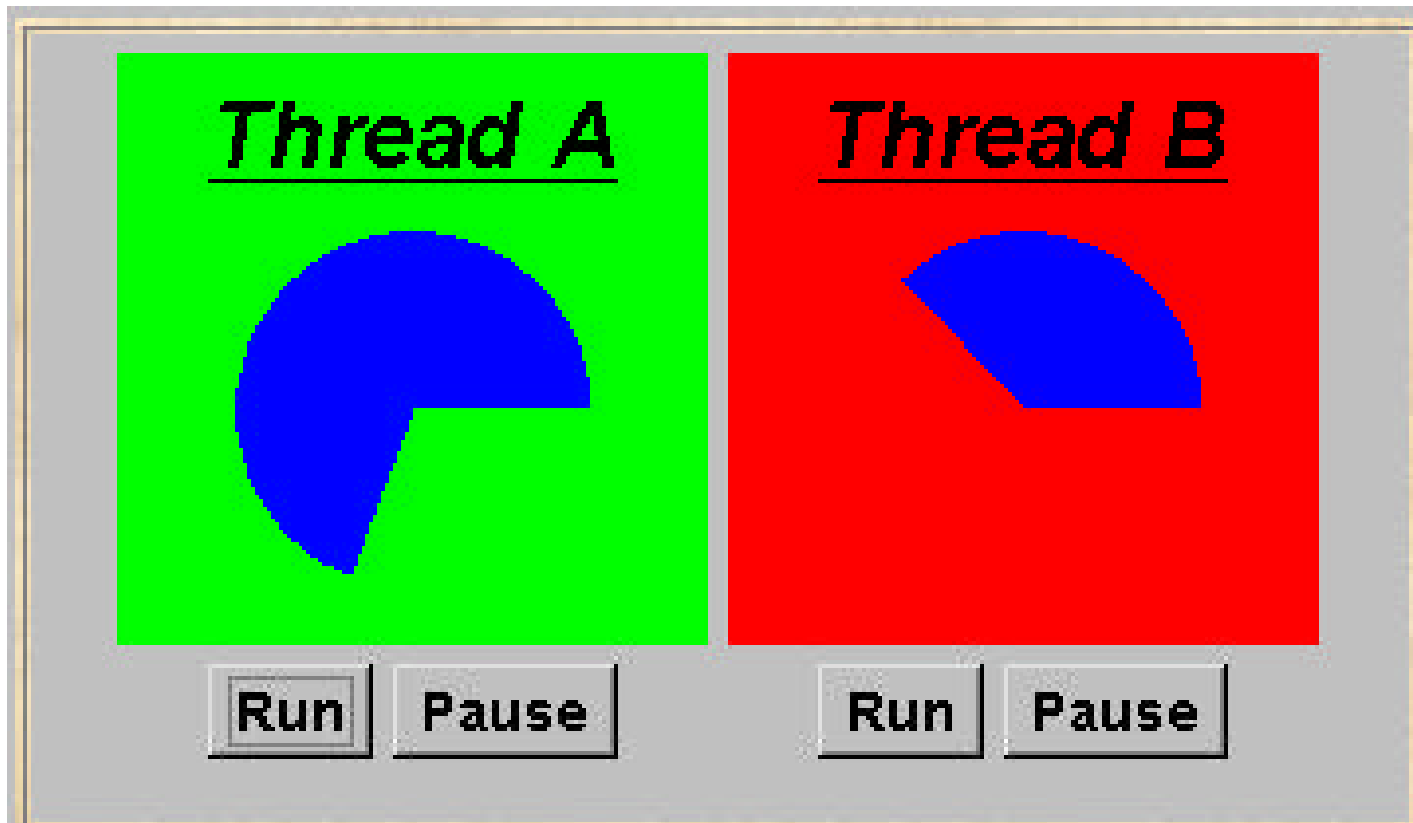
```
RESOURCE = (acquire->release->RESOURCE).  
USER = (printer.acquire->use  
->printer.release->USER).
```

```
|| PRINTER_SHARE  
= (a:USER || b:USER || {a,b}::printer:RESOURCE).
```

## 3.2 Multi-threaded Programs in Java

---

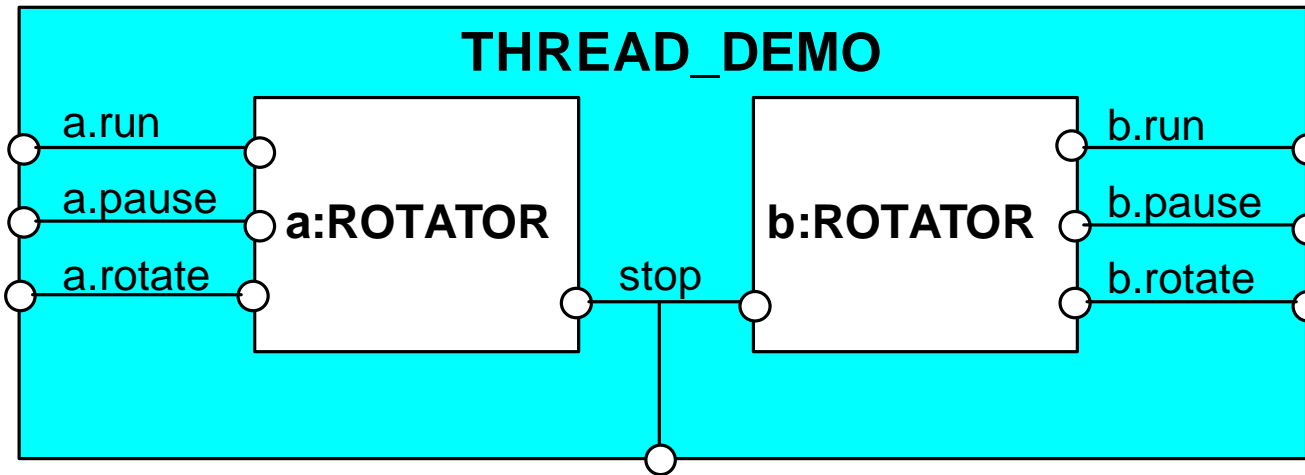
Concurrency in Java occurs when more than one thread is alive. ThreadDemo has two threads which rotate displays.



Concurrency: concurrent execution



# ThreadDemo model



```

ROTATOR = PAUSED,
PAUSED  = (run->RUN | pause->PAUSED
           | interrupt->STOP),
RUN     = (pause->PAUSED | {run,rotate}->RUN
           | interrupt->STOP).
    
```

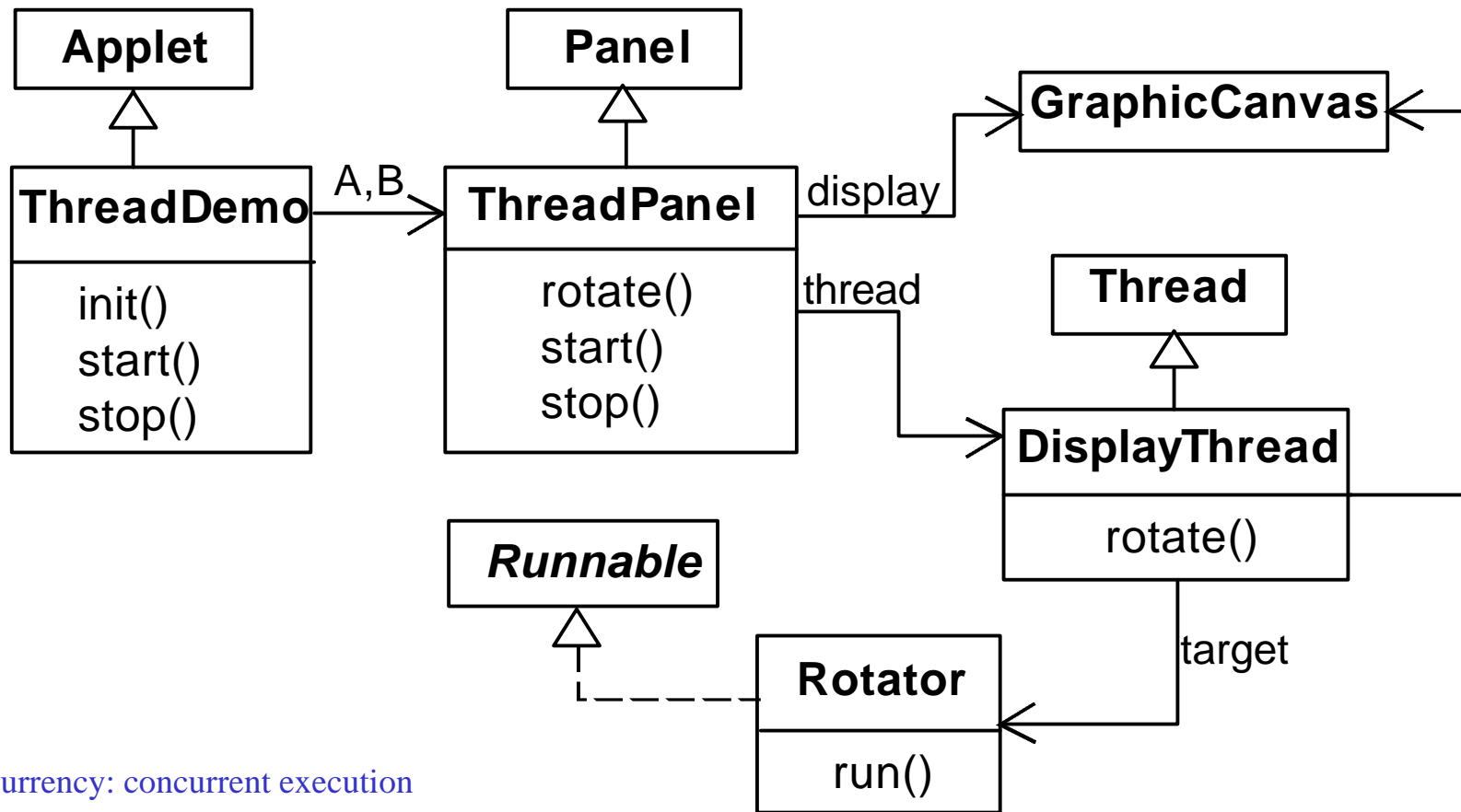
```

|| THREAD_DEMO = (a:ROTATOR || b:ROTATOR)
/ {stop / {a,b}.interrupt}.
    
```

*Interpret  
run,  
pause,  
interrupt  
as inputs,  
rotate as  
an output.*

# ThreadDemo implementation in Java - class diagram

**ThreadDemo** creates two **ThreadPanel** displays when initialized. **ThreadPanel** manages the display and control buttons, and delegates calls to **rotate()** to **DisplayThread**. **Rotator** implements the **Runnable** interface.



## Rotator class

---

```
class Rotator implements Runnable {  
    public void run() {  
        try {  
            while(true) ThreadPanel.rotate();  
        } catch(InterruptedException e) {}  
    }  
}
```

**Rotator** implements the **Runnable** interface, calling **ThreadPanel.rotate()** to move the display.

**run()** finishes if an exception is raised by **Thread.interrupt()**.

## ThreadPanel class

```
public class ThreadPanel extends Panel {  
  
    // construct display with title and segment color c  
    public ThreadPanel(String title, Color c) {...}  
  
    // rotate display of currently running thread 6 degrees  
    // return value not used in this example  
    public static boolean rotate()  
        throws InterruptedException {...}  
  
    // create a new thread with target r and start it running  
    public void start(Runnable r) {  
        thread = new DisplayThread(canvas, r, ...);  
        thread.start();  
    }  
  
    // stop the thread using Thread.interrupt()  
    public void stop() {thread.interrupt();}  
}
```

### ThreadPanel

manages the display and control buttons for a thread.

Calls to `rotate()` are delegated to `DisplayThread`.

Threads are created by the `start()` method, and terminated by the `stop()` method.

## ThreadDemo class

```
public class ThreadDemo extends Applet {
    ThreadPanel A; ThreadPanel B;

    public void init() {
        A = new ThreadPanel("Thread A",Color.blue);
        B = new ThreadPanel("Thread B",Color.blue);
        add(A); add(B);
    }

    public void start() {
        A.start(new Rotator());
        B.start(new Rotator());
    }

    public void stop() {
        A.stop();
        B.stop();
    }
}
```

**ThreadDemo** creates two **ThreadPanel** displays when initialized and two threads when started.

**ThreadPanel** is used extensively in later demonstration programs.

# Summary

---

## ◆ Concepts

- concurrent processes and process interaction

## ◆ Models

- **Asynchronous** (arbitrary speed) & **interleaving** (arbitrary order).
- **Parallel composition as a finite state process with action interleaving.**
- **Process interaction by shared actions.**
- **Process labeling and action relabeling and hiding.**
- **Structure diagrams**

## ◆ Practice

- **Multiple threads in Java.**

Concurrency: concurrent execution